Feature clustering and ranking for selecting stable features from high dimensional remotely sensed data

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High dimensional remote sensing data sets typically contain redundancy amongst the features. Traditional approaches to feature selection are prone to instability and selection of sub-optimal features in these circumstances. They can also be computationally expensive, especially when dealing with very large remote sensing datasets. This article presents an efficient, deterministic feature ranking method that is robust to redundancy. Affinity propagation is used to group correlated features into clusters. A relevance criterion is evaluated for each feature. Clusters are then ranked based on the median of the relevance values of their constituent features. Individual features can then be selected from the best clusters. Other criteria, such as computation time or measurement cost, can be considered when making this selection. The proposed feature selection method is compared to competing filter approach methods on a number of remote sensing data sets containing feature redundancy. Mutual information and naive Bayes relevance criteria were evaluated in conjunction with the feature selection methods. Using the proposed method it was shown that the stability of selected features improved under different data samplings, while similar or better classification accuracies were achieved compared to competing methods.

Keywords: feature selection; clustering; high dimensionality; redundancy; stability

# Introduction

In image classification, the amount of training data required to adequately represent class distributions in feature space increases exponentially as the number of features (variables) is increased – a phenomena known as the ‘curse of dimensionality’ (Bishop 2003). For finite training samples, increasing the features beyond a certain point results in overtraining and a decrease in the classifier accuracy. This so-called ‘peaking phenomenon’ (Jain, Duin, and Mao 2000) requires the size of the feature set to be reduced to a salient minimum in order to achieve an accurate classification. Support vector machine (SVM) (Burges 1998) and random forest (Breiman 2001) classifiers have become popular in remote sensing, partly because of their lack of sensitivity to the peaking phenomenon (Guyon et al. 2002), but several studies have demonstrated the benefits of feature reduction when these classifiers were applied to high-dimensional data (Guyon et al. 2002; Strobl et al. 2008; Tolosi and Lengauer 2011). Reducing the number of features is also beneficial from the perspective of measurement costs and feature computation time. This is particularly relevant in large scale remote sensing studies involving Very High Resolution (VHR) imagery, as vast quantities of data require processing.

Two basic approaches to feature set reduction exist: feature selection and feature extraction. In feature extraction the feature set is mapped into a new feature space of reduced dimensionality (Webb 2002). A major disadvantage of the feature extraction approach is that it requires measurements and computations to produce the full feature set, which can be prohibitively costly. Feature extraction also hinders interpretability as it alters the original representation of the features. A feature extraction approach was thus not followed in this study.

Feature selection involves the selection of a subset of features from the original set according to some criterion of subset performance. The number of possible subsets increases combinatorially with the size of the feature set and it is seldom practical to evaluate all possible subsets (Jain, Duin, and Mao 2000). A variety of search methods exists for reducing the portion of feature space searched. The fastest and most straightforward search method is simply to rank features based on their individual performance and select the best *N*. However, feature ranking approaches are problematic for data sets containing feature redundancy. In these situations, correlated features are ranked similarly, resulting in sub-optimal and redundant feature sets.

More advanced search methods use greedy sequential approaches, such as forward selection and backward elimination. Compared to the feature ranking approach, greedy search methods are more likely to find the globally optimal feature set as they explore more of the search space and are less inclined to select multiple redundant features (Webb 2002). The forward selection (FS) approach starts with an empty feature set and proceeds in a number of steps where one feature is added to the selected set at each step. The feature whose selection most improves an accuracy criterion is the one that is selected for that step. The selection process proceeds for a set number of steps or until a stopping criterion is reached (Bishop 2003). The backward elimination (BE) method starts with the full set of features and proceeds in a number of steps where one feature is eliminated from the selected set at each step. The feature whose removal produces the best accuracy according to some criterion is the one eliminated for that step. Again, the BE selection process proceeds for a set number of steps or until a stopping criterion is reached (Bishop 2003).

Feature selection methods can be grouped into filter, wrapper and embedded approaches. In the filter approach, generic measures of separability or importance are used to evaluate feature subsets, while in the wrapper approach, the accuracy of a specific classifier trained on the feature subset is used as the selection criterion (Duin and Tax 2005). An embedded approach is one where feature selection is incorporated into the classifier training procedure, such as with random forests (Breiman 2001). Filter approaches have the advantage over wrapper and embedded approaches of making feature selection independent of the classifier, thus allowing for greater flexibility in the choice of classifier (Brown et al. 2012). In general, filter approaches are also computationally more efficient than wrapper approaches. This is an important consideration for large and high dimensional data sets such as those often encountered in remote sensing. This study focuses on filter approaches.

High dimensional feature spaces typically contain feature redundancy (Cukur et al. 2015; Tolosi and Lengauer 2011; Yu and Liu 2004). Although feature correlation and redundancy are related, they are not strictly the same thing (Brown et al. 2012; Guyon and Elisseeff 2003). Features can help improve separability when the within class correlation is stronger than the between class correlation. We use the term ‘redundancy’ to refer to correlation of features between classes. The raw bands of multispectral imagery often have significant spectral overlap and consequently are correlated with one another. This spectral overlap will exacerbate the redundancy amongst features derived from these raw bands (Cukur et al. 2015). Hyperspectral imagery is also well-known for containing redundancy amongst the bands (Yuan, Zhu, and Wang 2015).

A number of authors have noted difficulties in selecting features from high dimensional data sets. Kononenko et al. (1997), Guyon et al. (2002), Yu & Liu (2004) and Yousef et al. (2007) noted that feature redundancy can have a negative impact on the optimality of feature selection. Feature redundancy not only leads to sub-optimal feature selection, but also makes selected features unstable and sensitive to small changes in the data used for selection (Tolosi and Lengauer 2011; Guyon and Elisseeff 2003; Li, Harner, and Adjeroh 2011; Kalousis, Prados, and Hilario 2007).

Redundancy can be effectively dealt with using a feature extraction approach, such as PCA, but this requires computation of the full feature set. This is not practical in computationally demanding applications such as analysing very high resolution (VHR) imagery over large areas.

The availability of high resolution imagery and associated feature extraction and classification techniques are rapidly increasing (Chi et al. 2016) resulting in large quantities of high spatial and spectral resolution data requiring interpretation. As the size of remote sensing data increases, computationally efficient feature selection techniques robust to high dimensional redundant spaces will become increasingly important. In this paper we propose a filter approach feature selection method for addressing the problems of redundancy and instability associated with high dimensional feature spaces of remotely sensed data. We adopt the filter approach due its relative speed and separation of feature selection and classification tasks. The method employs affinity propagation to identify clusters of redundant features. Redundancy is the removed or reduced by selecting a single representative feature for each cluster. Affinity propagation has the advantage of producing deterministic results and not requiring prior knowledge of the number of clusters. Correlation is used to measure feature similarity, which allows a broader encapsulation of feature redundancy than distance measures such as Euclidean distance, used by X. Chen et al. (2017). Assumptions of linear dependence between features and class labels made in structured sparsity regularisation approaches (Gui et al. 2016), are avoided by selecting features with a relevance heuristic based on the use of naïve Bayes or mutual information criteria.

The proposed method is unique in that it allows consideration of computation time and measurement cost in selecting features from correlated clusters of similarly relevant features. While many feature selection evaluations only consider classification accuracy (Yu and Liu 2004; Strobl et al. 2008; X. Chen et al. 2017), we present measures of computation time, classification accuracy and stability of selected features under different data samplings.

# Methods

## Related Work

## Feature Clustering and Ranking

The proposed method is described as follows:

1. Perform affinity propagation clustering (Frey and Dueck 2007) of the feature set using the absolute value of the correlation coefficient as the similarity metric.
2. Rank each cluster’s importance by finding the value of a relevance criterion for each individual feature and then finding the median of the feature relevance values in the cluster.
3. Select a single feature from each of the *N* clusters with best importance scores.

Affinity propagation is a clustering technique that identifies cluster representatives (‘exemplars’), and their corresponding clusters, by an iterative scheme of message passing between data points (Frey and Dueck 2007). A matrix of pair-wise similarities and a ‘preference’ parameter are required as inputs. The preference parameter affects the number of identified clusters and may be chosen automatically based on the values of the similarities. The proposed feature selection method sets the preference parameter to the median of the similarities, which results in a moderate number of clusters (Frey and Dueck 2007). Unlike clustering techniques such as *k*-means, affinity propagation does not require prior knowledge of the number of clusters.

Two kinds of messages, ‘availability’ and ‘responsibility’, are passed between data points at each iteration. The values of these messages reflect the current affinity one point has for choosing another as its exemplar. The responsibility reflects the accumulated evidence that feature *k* is the exemplar for feature *i*, taking into consideration other possible exemplars for feature *i*. The availability reflects the accumulated evidence for how appropriate it would be for feature *i* to choose feature *k* as its exemplar, taking into consideration support from other features for choosing *k* as their exemplar.

To initialise, the availabilities are set to zero, . The similarity *)* between feature *i* and *k*, is set to the absolute value of the correlation coefficient. The self- similarities, , are set to the preference value. At each iteration, the responsibilities are updated using the rule:

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| --- | --- |
|  | (1) |

The availabilities are correspondingly updated using the rule:

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|  | (2) |

The exemplar for feature *i* is identified by the value of *k* that maximizes . The iterations continue until the clusters (and their corresponding exemplars) remain stable for ten consecutive updates.

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We investigated the performance of two different feature relevance measures: the accuracy of a naive Bayes classifier and the mutual information (MI) between the feature and the class labels. The naive Bayes classifier, using a histogram to model class densities, was chosen primarily because it makes no assumptions about the form of the class distributions and can thus provide a generic measure of separability. It is simple, fast and recognised as being accurate for a variety of problems (Hand and Yu 2001). The ‘naive’ assumption of feature independence is of no consequence when testing individual features.

MI is a measure of the dependence between two random variables (Brown et al. 2012). Given two random variables and , with probability distributions and and joint probability distribution , the MI between and is defined as:

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|  | (3) |

The MI between a feature and the class labels gives a useful indication of that feature’s relevance or importance (Brown et al. 2012). The probability distributions in Equation (3) are not known and are estimated using histograms.

The cluster importance measure for the *k*th cluster can be expressed as

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|  | (3) |

where is the set of features in cluster *k and* is the feature relevance meaure for feature and class labels . For automatic feature selection, the feature with the maximum relevance measure in each of the *N* top ranked clusters is selected. When factors of measurement cost or computation time are to be

The number of clusters to select, *N*, can be specified by the user based on the size of the training set or by using a grid search with the final classifier accuracy as performance measure. To avoid biased accuracy estimates, all classifier accuracy evaluations, for cluster ranking or selection of *N*, are done on unseen test data using a five-fold cross validation (Bishop 2003).

## Data Sets

Five remote sensing and one synthetic data set were used for comparing the proposed method against popular existing feature selection methods. The data sets are detailed in Table 1. The ‘difficulty’ in the last column is calculated as , as in Brown et al. (2012), where is the number of objects, the number of features and the number of classes. Smaller values indicate that the data is less representative of the underlying class distributions, which results in more challenging feature selection and classification tasks. The Spekboom set consists of 46 spectral and textural features derived from four band multispectral, 0.5 m spatial resolution aerial imagery. The classes represent three types of vegetation found in the Little Karoo, a semi-arid region in South Africa. It was created as part of a vegetation mapping project being conducted by the authors.

The two class synthetic data set was generated to have redundancy amongst the features. The first five features for class were generated from a normal distribution, , with mean mean and standard deviation of one (). The mean, , of each distribution, was generated from the standard normal distribution, . The same number of objects were generated for each class. To introduce redundancy, an additional five features were generated by adding normally distributed noise, , to the original five features. A further five redundant features were similarly generated, but by adding normally distributed noise, , to the original features. Finally, two spurious features, sampled from a standard normal distribution, , were added to the data set.

The Statlog Landsat and Urban Land Cover data sets were obtained from the UCI Machine Learning Repository (Lichman 2013). The Statlog Landsat features are generated from six band multispectral pixel values in three by three neighbourhoods. The data set consists of six land cover classes. The features of the Urban Land Cover data set are comprised of multi-scale spectral, size, shape and textural measures, derived from high resolution aerial imagery (Johnson and Xie 2013).

Kennedy Space Centre (KSC) and Botswana are public hyperspectral data sets with vegetation and land cover classes (GIC 2014). The Botswana data were acquired by the Hyperion sensor on board the NASA EO-1 satellite and consist of 145 bands in the 400-2500 nm portion of the spectrum, at a 30 m pixel resolution. The KSC data were acquired by the NASA AVIRIS (Airborne Visible/Infrared Imaging Spectrometer) sensor and consist of 176 bands in the 400-2500 nm range, acquired at a spatial resolution of 18 m.

[Table 1. Data sets]

## Evaluation

The proposed Feature Clustering and Ranking (FCR) method was compared to a number of other established and competing feature selection methods. We adopted a similar, although reduced, evaluation approach to that of Brown et al. (2012) and Wu et al. (2013). The compared methods included the standard selection approaches of ranking, FS and BE. These standard approaches and FCR, were each evaluated with two different feature relevance criteria: MI and the naïve Bayes classification accuracy. The MI relevance criterion for FCR and ranking approaches finds the MI between individual features and the class labels. To integrate the MI relevance criterion into FS and BE, it is necessary to compute the MI of a set of multiple candidate features with the class labels. In this situation, the candidate features are first merged into a joint variable and then the MI of the class labels with this joint variable is computed (Brown et al. 2012). We used histograms with ten bins along each dimension to approximate probability densities for both the MI and naive Bayes criteria (Webb 2002). This approximation is made to avoid difficulties and inefficiencies associated with estimating probability densities for continuous variables (Brown et al. 2012).

In addition to the ranking, FS and BE approaches, two competing feature selection approaches, JMI and Mimimum-Redundancy Maximum-Relevance (mRMR),were included in our study to represent the ‘state of the art’ performance. Brown et al. (2012) compared the performance of several feature selection criteria in redundant high dimensional spaces, and found the JMI criterion gave the best overall performance in terms of classification accuracy and stability. The JMI measure for feature is

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|  | (4) |

where are the class labels and is the set of previously selected features. JMI considers the MI between the class labels and the joint variables , which are the pairwise combinations of the candidate feature with each feature already selected. It measures how well the candidate feature complements selected features in describing the class labels.

The popular mRMR criterion, introduced by (Peng, Long, and Ding 2005) expresses the trade-off between feature relevance and redundancy using mutual information measures. The mRMR measure for candidate feature is

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|  | (5) |

The first term expresses relevance as the dependence between the candidate feature and class labels, while the second term approximates the redundancy as the mean pair-wise dependencies between the candidate and previously selected features.

[Table 2. Method and criteria combination]

To quantify the stability of the selected features, we used the consistency index developed by Kuncheva (2007). If and and are subsets of the full feature set , with , and , the consistency index is

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|  | (5) |

It’s value lies in the range , where positive values indicate similar sets, zero indicates a random relation and negative values indicate an anti-correlation between the feature sets (Kuncheva 2007). To evaluate stability for a particular method, we select features from bootstrap samples of the data. The consistency index is found for each pairwise combination of selected features over ten bootstraps of the data and averaged to give a measure of overall stability.

A *k-*nearest-neighbour (*k-*NN) classifier (with ) was used to evaluate the accuracy of the features selected by each method. *k-*NN is a generic classifier that makes no assumptions about the data and requires no tuning. While other classifiers may be more accurate in particular situations, *k-*NN allows a relative comparison of the feature selection methods, independent of the influence of classifier tuning for specific data. For each of the feature sets found from the bootstrap samples, the *k-*NN accuracy was found as the average per-class accuracy from a ten-fold cross validation. For each method and data set combination, an overall accuracy was computed as the average of the bootstrap accuracies.

The number of features to select for each data set was fixed across methods. This parameter was selected by using the accuracy of a *k-*NN classifier (), trained on the first *N* features selected by FS-NaiveBC, as the criterion in a grid search. A low value of *N* that achieved good accuracy was selected for each data set.

The FCR methods (FCR-MI and FCR-NaiveBC) required some specific treatment to integrate them into the evaluation. After bootstrapping, clusters were assigned unique indices, ensuring identical clusters had the same index. The consistency index was then found using the selected cluster indices rather than feature indices. This was done to simulate hand-selection of preferred features from the best clusters for each bootstrap, while, in practice, allowing the FCR algorithm to automatically choose the top ranked feature from each cluster (for the sake of simplicity and speed). In other words, the cluster index was used to represent the index of the preferred feature that could otherwise have been selected by hand from the cluster contents.

We followed a similar approach to that of Brown et al. (2012), for computing a single ‘non-dominated’ ranking of the methods that considers stability and accuracy performance simultaneously. The concept of ‘Pareto optimality’, is used to find a single optimal solution in terms of multiple criteria. In the context of our evaluation, the ‘Pareto front’ is the set of methods on which no other method can improve without degrading either the accuracy or stability. The methods in this set are called ‘non-dominated’ (Mishra and Harit 2010). Successive Pareto fronts can be formed iteratively by finding the current Pareto front of the set of methods that excludes members of the previous fronts. A method was thus given a non-dominated rank of *N* if it was a member of the *N*th Pareto front. The average of the non-dominated ranks for each method over the six data sets was used to produce an overall ranking.

The bulk of the software implementation was done in MatlabTM, making use of the PRTools toolbox (TU Delft 2015). The MI, JMI and mRMR criteria were computed using the FEAST (FEAture Selection Toolbox) C++ implementation (Brown et al. 2012).

# Results and Discussion

The number of features selected for each data set are detailed in Table 3.

[Table 3. Feature selection parameters]

The results of the stability and accuracy evaluations for each method and data set combination are shown in Figure 1 and Figure 2 respectively. The methods appear along the x axis in order of their mean stability in Figure 1, and mean accuracy in Figure 2, over the six data sets. FS-MI was the most stable overall, but had one of the poorest accuracies. Similarly, FS-NaiveBC is the most accurate overall, but is the least stable. While neither FCR-NaiveBC nor FCR-MI achieve the best overall accuracy or stability, they are amongst the top three methods for both performance measures. The wide range of stabilities confirms the sensitivity of some methods to variations in the data. The method accuracies span a smaller range than the method stabilities. Nonetheless, there are substantial differences in accuracy between the best and worst methods. Compared to the other data sets, the stability of the Spekboom, Synthetic and Landsat data is noticeably superior. As reflected in the ‘difficulty’ values in Table 1, these data sets are more representative of the underlying distributions and are thus less sensitive to disturbances.

The ranking methods, Rank-MI and Rank-NaiveBC both have poor accuracy performance. This is expected as these methods do not consider feature complementarity and only measure relevance of features in isolation. The relatively poor accuracy and stability of FS-JMI was surprising in the context of the results of Brown et al. (2012), where it produced the best overall performance. Perhaps FS-JMI is more competitive when applied to higher dimensional data sets, containing hundreds or thousands of features, such as those that were used in Brown et al. (2012). The FS-JMI results nevertheless provide a benchmark that helps confirm the usefulness of the FCR method for the type of data investigated in our study.

As with classifier design, there is a ‘curse of dimensionality’ problem with computing the MI of joint variables. As the number of features increases, the number of objects needed to adequately represent the feature distribution increases exponentially (Brown et al. 2012). For this reason, the MI criterion is not well suited for evaluating the BE method, which requires computation of the relevance criterion for the full feature set. This likely explains the poor performance of BE-MI in terms of both accuracy and stability. Note that part of the motivation for the JMI formulation is to circumvent this kind of representivity issue by using a low dimensional approximation to MI.

[Figure 1. Method stability per data set (methods along the x axis are ordered by their mean stability over the data sets)]

[Figure 2. Method accuracy per data set (methods along the x axis are ordered by their mean accuracy over the data sets)]

The method execution times, summed over the six data sets, are provided for reference in Table 4. The execution time of FCR competes well with the other methods. The NaiveBC criterion is slower to compute than the MI criterion as it uses a five-fold cross-validation, implemented in MatlabTM, to evaluate the classification accuracy. MI is computed once-off using the efficient FEAST C++ implementation. Methods using the NaiveBC criterion are consequently slower than their MI counterparts. JMI is faster than the related FS-MI method, as the criterion only requires MI computations between pairwise combinations of features and the class labels, while the MI criterion is evaluated on the combination all selected features. BE is known to be less efficient than FS (Guyon and Elisseeff 2003), and is slowest of the tested methods.

[Table 4. Method cumulative execution time over all data]

Table 5 presents the non-dominant ranking of the methods, in terms of both accuracy and stability. The best ranked method overall is FCR-MI, with FCR-NaiveBC, FS-MI and FS-NaiveBC occupying the second rank position. While the FS-MI and FS-NaiveBC produced the best performance for stability and accuracy respectively, FCR-MI and FCR-NaiveBC achieved a better compromise between these two measures. The Rank-NaiveBC, Rank-MI and BE-MI methods are ranked lowest due to the known limitations of these methods.

If the clustering step were omitted, FCR-MI and FCR-NaiveBC would simplify to Rank-MI and Rank-NaiveBC respectively. FCR-MI and FCR-NaiveBC show a substantial improvement in performance compared to Rank-MI and Rank-NaiveBC which lends support to the effectiveness of the clustering step. Considering the combination of the MI and naive Bayes criteria with each method in isolation, there is a general trend for MI to produce better stability and naive Bayes to produce better accuracy. While FCR works well with either criterion, the results favour the use of MI as it is faster and produces a better non-dominant ranking than naive Bayes. On the whole the evaluation study shows the FCR method to be effective at selecting accurate and stable features from high dimensional remote sensing data containing redundancy.

[Table 5. Non-dominated ranking of methods by accuracy and stability]

# Conclusions

Small changes in data sets containing redundancy can result in substantial changes in selected features. Feature redundancy is also known to cause selection of sub-optimal features. A method for selecting stable and informative features from redundant data by ranking correlated clusters of features, was presented. Using hierarchical clustering, a natural number of clusters can be selected by observing the stability of correlation relationships in the data using a dendrogram. Clusters are then ranked using an importance measure, calculated as the median of a relevance criterion evaluated on each individual feature in the cluster. By selecting individual features from the best clusters, a set of informative features is found while simultaneously removing redundancy from the data. The ability to hand-pick features from the best clusters distinguishes FCR from related feature selection methods. This ability is beneficial as it allows other factors, such as speed of computation and physical interpretability, to be considered when determining an effective feature set.

FCR performed well on a diverse range of high dimensional redundant data sets. The effectiveness of the proposed FCR method was evaluated by comparing its accuracy, stability and execution time to a set of popular feature selection methods. The feature selection methods were each tested in combination with two criteria for feature relevance: the MI between the candidate feature(s) and the class labels, and the accuracy of a naive Bayes classifier trained on the candidate feature(s). Unlike structured sparsity regularisation approaches, these relevance criteria do not assume a linear dependence between features and class labels. FS-NaiveBC provided the best accuracy performance but the worst stability performance. In a similar vein, FS-MI provided the best stability performance but the second worst accuracy performance. The FCR method performed well overall, with both naive Bayes and MI criteria. Although FCR did not quite achieve the best performance in accuracy or stability alone, it was the highest ranked method when considering the accuracy and stability measures in combination. Another benefit of FCR is its relative speed compared to greedy search FS and BE type methods. Ever increasing quantities of high spatial and spectral resolution remote sensing data are being produced and require interpretation (Chi et al. 2016). In this context, instability and sub-optimality associated with feature selection from high dimensional redundant data will become increasingly critical issues. Computationally efficient techniques, such as FCR, are required to address these challenges.

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