Feature clustering and ranking for selecting stable features from high dimensional remotely sensed data

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High dimensional remote sensing data sets typically contain redundancy amongst the features. Traditional approaches to feature selection are prone to instability and selection of sub-optimal features in these circumstances. They can also be computationally expensive, especially when dealing with very large remote sensing datasets. This article presents an efficient, deterministic feature ranking method that is robust to redundancy. Affinity propagation is used to group correlated features into clusters. A relevance criterion is evaluated for each feature. Clusters are then ranked based on the median of the relevance values of their constituent features. The most relevant individual features can then be selected automatically from the best clusters. Other criteria, such as computation time or measurement cost, can optionally be considered interactively when making this selection. The proposed feature selection method is compared to competing filter approach methods on a number of remote sensing data sets containing feature redundancy. Mutual information and naive Bayes relevance criteria were evaluated in conjunction with the feature selection methods. Using the proposed method it was shown that the stability of selected features improved under different data samplings, while similar or better classification accuracies were achieved compared to competing methods.

Keywords: feature selection; clustering; high dimensionality; redundancy; stability

# Introduction

In image classification, the amount of training data required to adequately represent class distributions in feature space increases exponentially as the number of features (variables) is increased – a phenomena known as the ‘curse of dimensionality’ (Bishop 2003). For finite training samples, increasing the features beyond a certain point results in overtraining and a decrease in the classifier accuracy. This so-called ‘peaking phenomenon’ (Jain, Duin, and Mao 2000) requires the size of the feature set to be reduced to a salient minimum in order to achieve an accurate classification. Support vector machine (SVM) (Burges 1998) and random forest (Breiman 2001) classifiers have become popular in remote sensing, partly because of their lack of sensitivity to the peaking phenomenon (Guyon et al. 2002), but several studies have demonstrated the benefits of feature reduction when these classifiers were applied to high-dimensional data (Guyon et al. 2002; Strobl et al. 2008; Tolosi and Lengauer 2011). Reducing the number of features is also beneficial from the perspective of measurement costs and feature computation time. This is particularly relevant in large scale remote sensing studies involving Very High Resolution (VHR) imagery, as vast quantities of data require processing.

Two basic approaches to feature set reduction exist: feature selection and feature extraction. In feature extraction the feature set is mapped into a new feature space of reduced dimensionality (Webb 2002). A major disadvantage of the feature extraction approach is that it requires measurements and computations to produce the full feature set, which can be prohibitively costly. Feature extraction also hinders interpretability as it alters the original representation of the features. A feature extraction approach was thus not followed in this study.

Feature selection involves the selection of a subset of features from the original set according to some criterion of subset performance. The number of possible subsets increases combinatorially with the size of the feature set and it is seldom practical to evaluate all possible subsets (Jain, Duin, and Mao 2000). A variety of search schemes exist for reducing the portion of feature space searched. The fastest and most straightforward search scheme is simply to rank features based on their individual performance and select the best *N*. However, feature ranking approaches are problematic for data sets containing feature redundancy. In these situations, correlated features are ranked similarly, resulting in sub-optimal and redundant feature sets.

More advanced feature selection search schemes use greedy sequential approaches, such as forward selection and backward elimination. Compared to the feature ranking approach, greedy search procedures are more likely to find the globally optimal feature set as they explore more of the search space and are less inclined to select multiple redundant features (Webb 2002). The forward selection (FS) approach starts with an empty feature set and proceeds in a number of steps where one feature is added to the selected set at each step. The feature whose selection most improves an accuracy criterion is the one that is selected for that step. The selection process proceeds for a set number of steps or until a stopping criterion is reached (Bishop 2003). The backward elimination (BE) method starts with the full set of features and proceeds in a number of steps where one feature is eliminated from the selected set at each step. The feature whose removal produces the best accuracy according to some criterion is the one eliminated for that step. Again, the BE selection process proceeds for a set number of steps or until a stopping criterion is reached (Bishop 2003). BE is computationally more costly than FS as it begins evaluation on the full feature set. For the same reason, it also requires adequate data to represent the full feature set.

Feature selection methods can be grouped into filter, wrapper and embedded approaches. In the filter approach, generic measures of separability or importance are used to evaluate feature subsets, while in the wrapper approach, the accuracy of a specific classifier trained on the feature subset is used as the selection criterion (Duin and Tax 2005). An embedded approach is one where feature selection is incorporated into the classifier training procedure, such as with random forests (Breiman 2001). Filter approaches have the advantage over wrapper and embedded approaches of making feature selection independent of the classifier, thus allowing for greater flexibility in the choice of classifier (Brown et al. 2012). In general, filter approaches are also computationally more efficient than wrapper approaches. This is an important consideration for large and high dimensional data sets such as those often encountered in remote sensing. This study thus focuses on filter approaches.

High dimensional feature spaces typically contain feature redundancy (Cukur et al. 2015; Tolosi and Lengauer 2011; Yu and Liu 2004). Although feature correlation and redundancy are related, they are not strictly the same thing (Brown et al. 2012; Guyon and Elisseeff 2003). Features can help improve separability when the within class correlation is stronger than the between class correlation. We use the term ‘redundancy’ to refer to correlation of features between classes. The raw bands of multispectral imagery often have significant spectral overlap and consequently are correlated with one another. This spectral overlap will exacerbate the redundancy amongst features derived from these raw bands (Cukur et al. 2015). Hyperspectral imagery is also well-known for containing redundancy amongst the bands (Yuan, Zhu, and Wang 2015).

A number of authors have noted difficulties in selecting features from high dimensional data sets. Kononenko et al. (1997), Guyon et al. (2002), Yu & Liu (2004) and Yousef et al. (2007) noted that feature redundancy can have a negative impact on the optimality of feature selection. Feature redundancy not only leads to sub-optimal feature selection, but also makes selected features unstable and sensitive to small changes in the data used for selection (Tolosi and Lengauer 2011; Guyon and Elisseeff 2003; Li, Harner, and Adjeroh 2011; Kalousis, Prados, and Hilario 2007).

The increasing availability of high resolution imagery necessitates computationally efficient feature selection techniques robust to high dimensional redundant spaces. In this article we propose a computationally-efficient filter approach feature selection method for addressing the problems of sub-optimality and instability associated with high dimensional, redundant feature spaces of remotely sensed data. We adopt the filter approach due its separation of feature selection and classification tasks. The method employs affinity propagation to identify clusters of redundant features and redundancy is reduced by selecting a single representative feature from the most relevant clusters. The method requires no prior knowledge of the number of clusters. Correlation is used to measure feature similarity, which allows a broader encapsulation of feature redundancy than distance measures such as Euclidean distance (Chen et al. 2017). Assumptions of linear dependence between features and class labels made in structured sparsity regularisation approaches (Gui et al. 2016) are also avoided by selecting features with a relevance heuristic, based on the use of naïve Bayes or mutual information criteria. The proposed method can be fully automated, or it can be used interactively to allow for consideration of computation time and measurement cost. Tis compared The various feature selection methods are evaluated based on computation time, classification accuracy and stability of selected features under different data samplings.

# Methods

## Related Work

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(Wang et al. 2010; Chen and Gu 2015; Chen et al. 2017; Gui et al. 2016)

## Feature Clustering and Ranking

Within the context of the related research overviewed in the previous section, our proposed feature selection method consists of the following three steps:

1. Perform affinity propagation clustering (Frey and Dueck 2007) of the feature set using the absolute value of the correlation coefficient as the similarity metric.
2. Rank each cluster’s importance by finding the value of a relevance criterion for each individual feature and then finding the median of the feature relevance values in the cluster.
3. Select a single feature from each of the *N* clusters with best importance scores.

Affinity propagation is a clustering technique that identifies cluster representatives (‘exemplars’), and their corresponding clusters, by an iterative scheme of message passing between data points (Frey and Dueck 2007). A matrix of pair-wise similarities and a ‘preference’ parameter are required as inputs. The preference parameter affects the number of identified clusters and may be chosen automatically based on the values of the similarities. The proposed feature selection method sets the preference parameter to the median of the similarities, which results in a moderate number of clusters (Frey and Dueck 2007). Unlike clustering techniques such as *k*-means, affinity propagation does not require prior knowledge of the number of clusters.

Two kinds of messages, ‘availability’ and ‘responsibility’, are passed between data points at each iteration. The values of these messages express the current affinity one point has for choosing another as its exemplar. The responsibility reflects the accumulated evidence that feature *k* is the exemplar for feature *i*, taking into consideration other possible exemplars for feature *i*. The availability reflects the accumulated evidence for how appropriate it would be for feature *i* to choose feature *k* as its exemplar, taking into consideration support from other features for choosing *k* as their exemplar.

To initialise, the availabilities are set to zero, . In our method, the similarity *)* between feature *i* and *k*, is set to the absolute value of the correlation coefficient, and the self-similarities, , are set to the preference value. At each iteration, the responsibilities are updated using the rule:

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|  | (1) |

The availabilities are correspondingly updated using the rule:

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|  | (2) |

The exemplar for feature *i* is identified by the value of *k* that maximises . The iterations continue until the clusters (and their corresponding exemplars) remain stable for ten consecutive updates.

We investigated the performance of two different feature relevance measures: the accuracy of a naive Bayes classifier and the mutual information (MI) between the feature and the class labels. The naive Bayes classifier, using a histogram to model class densities, was chosen primarily because it makes no assumptions about the form of the class distributions and can thus provide a generic measure of separability. It is simple, fast and recognised as being accurate for a variety of problems (Hand and Yu 2001). The ‘naive’ assumption of feature independence is of no consequence when testing individual features.

MI is a measure of the dependence between two random variables (Brown et al. 2012). Given two random variables and , with probability distributions and and joint probability distribution , the MI between and is defined as:

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|  | (3) |

The MI between a feature and the class labels gives a useful indication of that feature’s relevance or importance (Brown et al. 2012). The probability distributions in Equation (3) are not known and are estimated using histograms.

The cluster importance measure for the *k*th cluster is expressed as

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|  | (4) |

where is the set of features in cluster *k and* is the MI or naïve Bayes feature relevance measure for feature and class labels . Once the clusters of similarly relevant features have been ranked according to their importance measures, single features may be selected from the best clusters using an automatic procedure or by the user, taking measurement cost and computation time into account. For automatic feature selection, the feature with the maximum relevance measure is selected from each of the *N* best clusters. When criteria of measurement cost or computation time require consideration, the user should hand select features minimising these costs from the *N* best clusters.

The number of clusters to select, *N*, can be specified by the user based on the size of the training set or by using a grid search with the final classifier accuracy as performance measure. To avoid biased accuracy estimates, all classifier accuracy evaluations, for cluster ranking or selection of *N*, are done on unseen test data using a five-fold cross validation (Bishop 2003).

## Data Sets

Five remote sensing and one synthetic data set (Table 1) were used for comparing the proposed method against popular existing feature selection methods. The ‘difficulty’ in the last column of Table 1 is calculated as , as in Brown et al. (2012), where is the number of objects, the number of features and the number of classes. Smaller values indicate that the data is less representative of the underlying class distributions, which results in more challenging feature selection and classification tasks. The Spekboom set consists of 46 spectral and textural features derived from four band multispectral, 0.5 m spatial resolution aerial imagery. The classes represent three types of vegetation found in the Little Karoo, a semi-arid region in South Africa. It was created as part of a vegetation mapping project being conducted by the authors.

The two class synthetic data set was generated to have redundancy amongst the features. The first five features for class were generated from a normal distribution, , with mean and standard deviation of one (). The mean, , of each distribution, was generated from the standard normal distribution, . The same number of objects were generated for each class. To introduce redundancy, an additional five features were generated by adding normally distributed noise, , to the original five features. A further five redundant features were similarly generated, but by adding normally distributed noise, , to the original features. Finally, two spurious features, sampled from a standard normal distribution, , were added to the data set.

The Statlog Landsat and Urban Land Cover data sets were obtained from the UCI Machine Learning Repository (Lichman 2013). The Statlog Landsat features are generated from six band multispectral pixel values in three by three neighbourhoods. The data set consists of six land cover classes. The features of the Urban Land Cover data set are comprised of multi-scale spectral, size, shape and textural measures, derived from high resolution aerial imagery (Johnson and Xie 2013).

Kennedy Space Centre (KSC) and Botswana are public hyperspectral data sets with vegetation and land cover classes (GIC 2014). The Botswana data were acquired by the Hyperion sensor on board the NASA EO-1 satellite and consist of 145 bands in the 400-2500 nm portion of the spectrum, at a 30 m pixel resolution. The KSC data were acquired by the NASA AVIRIS (Airborne Visible/Infrared Imaging Spectrometer) sensor and consist of 176 bands in the 400-2500 nm range, acquired at a spatial resolution of 18 m.

[Table 1. Data sets]

## Experimental design

The proposed Feature Clustering and Ranking (FCR) method was compared to a number of other established and competing feature selection methods. We adopted a similar, although reduced, evaluation approach to that of Brown et al. (2012) and Wu et al. (2013). The compared methods included the standard search approaches of ranking, FS and BE. These standard approaches and FCR, were each evaluated with two different feature relevance criteria: MI and the naïve Bayes classification accuracy. The MI relevance criterion for FCR and ranking approaches finds the MI between individual features and the class labels. To integrate the MI relevance criterion into FS and BE, it is necessary to compute the MI of a set of multiple candidate features with the class labels. In this situation, the candidate features are first merged into a joint variable and then the MI of the class labels with this joint variable is computed (Brown et al. 2012). We used histograms with ten bins along each dimension to approximate probability densities for both the MI and naive Bayes criteria (Webb 2002), to avoid difficulties and inefficiencies associated with estimating probability densities for continuous variables (Brown et al. 2012).

In addition to the MI and naive Bayes criteria, two other criteria, namely JMI and maximum relevance minimum redundancy (mRMR), were included in our study to represent ‘state of the art’ performance. Brown et al. (2012) compared the performance of several feature selection criteria in redundant high dimensional spaces, and found the JMI criterion gave the best overall performance in terms of classification accuracy and stability. The JMI measure for feature is

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|  | (5) |

where are the class labels and is the set of previously selected features. JMI considers the MI between the class labels and the joint variables , which are the pairwise combinations of the candidate feature with each feature already selected. It measures how well the candidate feature complements selected features in describing the class labels.

The popular mRMR criterion, introduced by Peng, Long, and Ding (2005), expresses the trade-off between feature relevance and redundancy using mutual information measures. The mRMR measure for candidate feature is

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|  | (6) |

The first term expresses relevance as the dependence between the candidate feature and class labels, while the second term approximates the redundancy as the mean pair-wise dependencies between the candidate and previously selected features. The JMI and mRMR criteria are used in a FS search scheme. Table 2 In this evaluation, the term ‘method’ is used to refer to a combination of search scheme, such as FS, and criterion, such as JMI.

[Table 2. Methods as combinations of search schemes and criteria]

To quantify the stability of the selected features, we used the consistency index developed by Kuncheva (2007). If and and are subsets of the full feature set , with , and , the consistency index is

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|  | (7) |

It’s value lies in the range , where positive values indicate similar sets, zero indicates a random relation and negative values indicate an anti-correlation between the feature sets (Kuncheva 2007). To evaluate stability for a particular method, we select features from bootstrap samples of the data. The consistency index is found for each pairwise combination of selected features over ten bootstraps of the data and averaged to give a measure of overall stability.

A *k-*nearest-neighbour (*k-*NN) classifier (with ) was used to evaluate the accuracy of the features selected by each method. *k-*NN is a generic classifier that makes no assumptions about the data and requires no tuning. While other classifiers may be more accurate in particular situations, *k-*NN allows a relative comparison of the feature selection methods, independent of the influence of classifier tuning for specific data. For each of the feature sets found from the bootstrap samples, the *k-*NN accuracy was found as the average per-class accuracy from a ten-fold cross validation. For each method and data set combination, an overall accuracy was computed as the average of the bootstrap accuracies.

The number of features to select for each data set was fixed across methods. This parameter was selected by using the accuracy of a *k-*NN classifier (), trained on the first *N* features selected by FS-NaiveBC, as the criterion in a grid search. A low value of *N* that achieved good accuracy was selected for each data set. The number of features selected for each data set are detailed in Table 3.

[Table 3. Feature selection parameters]

The FCR methods (FCR-MI and FCR-NaiveBC) required some specific treatment to integrate them into the evaluation. After bootstrapping, clusters were assigned unique indices, ensuring identical clusters had the same index. The consistency index was then found using the selected cluster indices rather than feature indices. This was done to simulate hand-selection of preferred features from the best clusters for each bootstrap, while allowing the FCR algorithm to automatically choose the top ranked feature from each cluster (for the sake of simplicity and speed). In other words, the cluster index was used to represent the index of the preferred feature that could otherwise have been selected by hand from the cluster contents.

We followed a similar approach to that of Brown et al. (2012) for computing a single ‘non-dominated’ ranking of the methods that considers stability and accuracy performance simultaneously. The concept of ‘Pareto optimality’ was used to find a single optimal solution in terms of multiple criteria. In the context of our evaluation, the ‘Pareto front’ is the set of methods on which no other method can improve without degrading either the accuracy or stability. The methods in this set are called ‘non-dominated’ (Mishra and Harit 2010). Successive Pareto fronts can be formed iteratively by finding the current Pareto front of the set of methods that excludes members of the previous fronts. A method was thus given a non-dominated rank of *N* if it was a member of the *N*th Pareto front. The average of the non-dominated ranks for each method over the six data sets was used to produce an overall ranking.

The bulk of the software implementation was done in MatlabTM, making use of the PRTools toolbox (TU Delft 2015). The MI, JMI and mRMR criteria were computed using the FEAST (FEAture Selection Toolbox) C++ implementation (Brown et al. 2012).

# Results and Discussion

The results of the stability and accuracy evaluations for each method and data set combination are shown in Figure 1 and Figure 2 respectively. The methods appear along the x axis in order of their mean stability in Figure 1, and mean accuracy in Figure 2, over the six data sets. The wide range of stabilities confirms the sensitivity of some methods to variations in the data. The method accuracies span a smaller range than the method stabilities. Nonetheless, there were substantial differences in accuracy between the best and worst methods. Compared to the other data sets, the stability of the Spekboom, Synthetic and Landsat data was noticeably superior. As reflected in the ‘difficulty’ values in Table 1, these data sets are more representative of the underlying distributions and are thus less sensitive to disturbances.

FCR-NaiveBC and FCR-MI occupy the top two positions for both performance measures. The ranking methods, Rank-MI and Rank-NaiveBC both had poor accuracy performance. This was expected as these methods do not consider feature complementarity and only measure relevance of features in isolation. The relatively poor accuracy and stability of FS-JMI was surprising in the context of the results of Brown et al. (2012), where it produced the best overall performance. The FS-JMI results nevertheless provide a benchmark that helps confirm the usefulness of the FCR method for the type of data investigated in our study.

As with classifier design, there is a ‘curse of dimensionality’ problem with computing the MI of joint variables. As the number of features increases, the number of objects needed to adequately represent the feature distribution increases exponentially (Brown et al. 2012). For this reason, the MI criterion is not well suited for evaluating the BE search scheme, which requires computation of the relevance criterion for the full feature set. This likely explains the poor performance of BE-MI in terms of both accuracy and stability. Part of the motivation for the JMI and mRMR formulations is to circumvent this kind of representivity issue by using a low dimensional approximation to MI.

[Figure 1. Method stability per data set (methods along the x axis are ordered by their mean stability over the data sets)]

[Figure 2. Method accuracy per data set (methods along the x axis are ordered by their mean accuracy over the data sets)]

The method execution times, summed over the six data sets, are provided in Table 4. The execution time of FCR competed well with the other methods, although mRMR was the fastest overall. The naïve Bayes criterion is slower to compute than the MI criterion as it uses a five-fold cross-validation to evaluate the classification accuracy, while MI is computed once-off. Methods using the naïve Bayes criterion are consequently slower than their MI counterparts. FS-JMI is faster than the related FS-MI method, as the criterion only requires MI computations between pairwise combinations of features and the class labels, while the MI criterion is evaluated on the combination all selected features. BE is known to be less efficient than FS (Guyon and Elisseeff 2003), and was the slowest of the tested search schemes.

[Table 4. Method cumulative execution time over all data]

Table 5 presents the non-dominant ranking of the methods, in terms of both accuracy and stability. The best ranked method overall was FCR-MI, followed by FCR-NaiveBC. The Rank-NaiveBC, Rank-MI, BE-NaiveBC and BE-MI methods were ranked lowest due to the known limitations of these methods. The FS-MRMR method was competitive on all measures, and was the third ranked method overall.

If the clustering step were omitted, FCR-MI and FCR-NaiveBC would simplify to Rank-MI and Rank-NaiveBC respectively. FCR-MI and FCR-NaiveBC showed a substantial improvement in performance compared to Rank-MI and Rank-NaiveBC, which lends support to the effectiveness of the clustering step. Considering the combination of the MI and naive Bayes criteria with each search scheme in isolation, there was a general trend for MI to produce better stability and naive Bayes to produce better accuracy. While FCR worked well with either criterion, the results favoured the use of MI as it is faster and produced a better non-dominant ranking than naive Bayes. On the whole, the evaluations demonstrate that the proposed FCR method is effective at selecting accurate and stable features from high dimensional remote sensing data containing redundancy.

[Table 5. Non-dominated ranking of methods by accuracy and stability]

# Conclusions

Small changes in data sets containing redundancy can result in substantial changes in selected features. Feature redundancy is also known to cause selection of sub-optimal features. This study presented and evaluated a new method for selecting stable and informative features from redundant data by ranking correlated clusters of features. The method uses affinity propagation to identify a moderate number of clusters of correlated and similarly relevant features. It then ranks the clusters using an importance measure, calculated as the median of a relevance criterion evaluated on each individual feature in the cluster. By selecting individual features from the best clusters, a set of informative features is found while simultaneously removing redundancy from the data. These features may be selected automatically based on their relevance, or interactively, taking criteria such as computation time and measurement cost into account. The option to include factors other than relevance and redundancy in determining selected features distinguishes FCR from related feature selection methods; although currently this option is limited to a manual procedure. Future work will investigate ways of combining relevance with other criteria to allow feature selection without user input.

The effectiveness of the proposed FCR method was evaluated by comparing its accuracy, stability and execution time to a set of popular feature selection methods. Two criteria were tested for measuring feature relevance: the MI between the candidate feature(s) and the class labels, and the accuracy of a naive Bayes classifier trained on the candidate feature(s). Unlike structured sparsity regularisation approaches, these relevance criteria do not assume a linear dependence between features and class labels. FCR performed well overall, with both naive Bayes and MI criteria and was the highest ranked method when considering the accuracy and stability measures in combination. Another benefit of FCR is its relative speed compared to greedy search FS and BE type methods. Ever increasing quantities of high spatial and spectral resolution remote sensing data are being produced and require interpretation (Chi et al. 2016). In this context, instability and sub-optimality associated with feature selection from high dimensional redundant data will become increasingly important. Computationally efficient techniques, such as FCR, are required to address these challenges.

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